

**Find the unknown side lengths in each special right triangle.**

1. A  $30^\circ$ - $60^\circ$ - $90^\circ$  triangle with hypotenuse 2 ft.

2. A  $45^\circ$ - $45^\circ$ - $90^\circ$  triangle with leg length 4 in.

3. A  $30^\circ$ - $60^\circ$ - $90^\circ$  triangle with longer leg length 3m

- I can develop and apply the formulas for the area and circumference of a circle.
- I can develop and apply the formula for the area of a regular polygon.

Vocabulary		
circle	center of a circle	center of a regular polygon
apothem	central angle of a regular polygon	

**Common Core: CC.9-12.G.GMD.1** Give an informal argument for the formulas for the circumference of a circle, area of a circle, volume of a cylinder, pyramid, and cone.

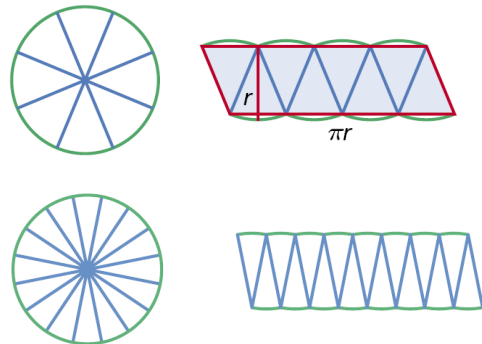
4. What is a circle?

**5.** What is  $\pi$ ?

6. What is the formula for the circumference of a circle?

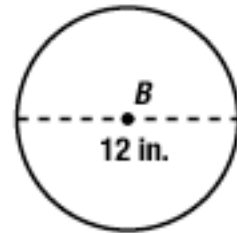
You can use the circumference of a circle to find its area. Divide the circle and rearrange the pieces to make a shape that resembles a parallelogram.

7. What is the formula for the area of a circle?



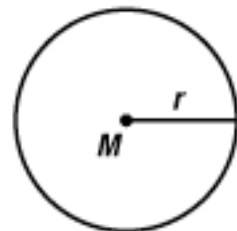
**Video Example 1.**

A) Find the area of  $\odot B$  in terms of  $\pi$ .



B) Find the radius of  $\odot Y$  in which  $C = 32\pi$  cm.

C) Find the circumference of  $\odot M$  if the area is  $A = 4x^2\pi m^2$ .



## 1 Finding Measurements of Circles

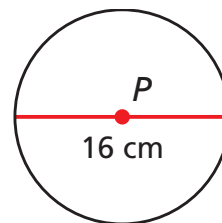
Find each measurement.

**A** the area of  $\odot P$  in terms of  $\pi$

$$A = \pi r^2 \quad \text{Area of a circle}$$

$$A = \pi(8)^2 \quad \text{Divide the diameter by 2 to find the radius, 8.}$$

$$A = 64\pi \text{ cm}^2 \quad \text{Simplify.}$$



Find each measurement.

**B** the radius of  $\odot X$  in which  $C = 24\pi$  in.

$$C = 2\pi r \quad \text{Circumference of a circle}$$

$$24\pi = 2\pi r \quad \text{Substitute } 24\pi \text{ for } C.$$

$$r = 12 \text{ in.} \quad \text{Divide both sides by } 2\pi.$$

**C** the circumference of  $\odot S$  in which  $A = 9x^2 \pi \text{ cm}^2$

**Step 1** Use the given area to solve for  $r$ .

$$A = \pi r^2 \quad \text{Area of a circle}$$

$$9x^2\pi = \pi r^2 \quad \text{Substitute } 9x^2\pi \text{ for } A.$$

$$9x^2 = r^2 \quad \text{Divide both sides by } \pi.$$

$$3x = r \quad \text{Take the square root of both sides.}$$

**Step 2** Use the value of  $r$  to find the circumference.

$$C = 2\pi r$$

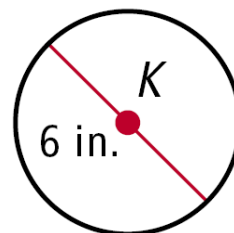
$$C = 2\pi(3x) \quad \text{Substitute } 3x \text{ for } r.$$

$$C = 6x\pi \text{ cm} \quad \text{Simplify.}$$



**Example 1.**

A. Find the area of  $\odot K$  in terms of  $\pi$ .



**B.** Find the area of  $\odot J$  if the circumference is  $(65x + 14)\pi$  *m*.

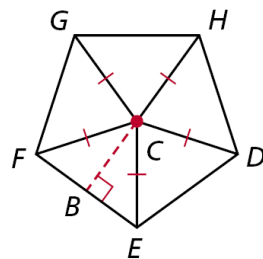
C. Find the circumference of  $\odot M$  if the area is  $25x^2\pi \text{ ft}^2$

8. **Guided Practice:** Find the area of  $\odot A$  in terms of  $\pi$  in which  $C = (4x - 6)\pi$  m.

### Helpful Hint

The  $\pi$  key gives the best possible approximation for  $\pi$  on your calculator. Always wait until the last step to round.

9. What is a regular polygon?



10. What is the center of the regular polygon?

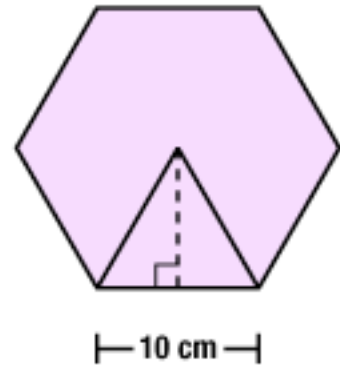
**11.** Compare and contrast the apothem and radius of a regular polygon.

**12.** How do you find the central angle of a regular polygon?

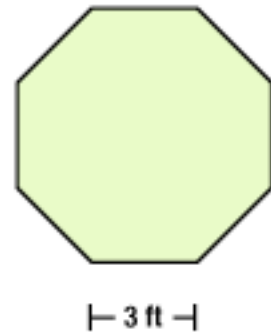
**13.** How do you find the area of a regular polygon?

**Video Example 3**

A) Find the area of polygon.



B) Find the area of polygon.



### 3 Finding the Area of a Regular Polygon

Find the area of each regular polygon. Round to the nearest tenth.

**A** a regular hexagon with side length 6 m

The perimeter is  $6(6) = 36$  m. The hexagon can be divided into 6 equilateral triangles with side length 6 m. By the  $30^\circ$ - $60^\circ$ - $90^\circ$  Triangle Theorem, the apothem is  $3\sqrt{3}$  m.

$$A = \frac{1}{2}aP$$

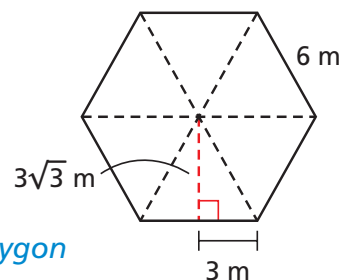
*Area of a regular polygon*

$$A = \frac{1}{2}(3\sqrt{3})(36)$$

*Substitute  $3\sqrt{3}$  for  $a$  and 36 for  $P$ .*

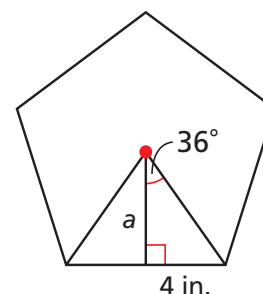
$$A = 54\sqrt{3} \cong 93.5 \text{ m}^2$$

*Simplify.*



**B** a regular pentagon with side length 8 in.

**Step 1** Draw the pentagon. Draw an isosceles triangle with its vertex at the center of the pentagon. The central angle is  $\frac{360^\circ}{5} = 72^\circ$ . Draw a segment that bisects the central angle and the side of the polygon to form a right triangle.



**Step 2** Use the tangent ratio to find the apothem.

$$\tan 36^\circ = \frac{4}{a}$$

*The tangent of an angle is  $\frac{\text{opp. leg}}{\text{adj. leg}}$ .*

$$a = \frac{4}{\tan 36^\circ}$$

*Solve for  $a$ .*

**Step 3** Use the apothem and the given side length to find the area.

$$A = \frac{1}{2}aP$$

*Area of a regular polygon*

$$A = \frac{1}{2}\left(\frac{4}{\tan 36^\circ}\right)(40)$$

*The perimeter is  $8(5) = 40$  in.*

$$A \cong 110.1 \text{ in}^2$$

*Simplify. Round to the nearest tenth.*

## Remember!

The tangent of an angle in a right triangle is the ratio of the opposite leg length to the adjacent leg length. See page 525.



**Example 3.**

- A. Find the area of regular heptagon with side length 2 ft to the nearest tenth.

**B.** Find the area of a regular dodecagon with side length 5 cm to the nearest tenth.

**14. Guided Practice:** Find the area of a regular octagon with a side length of 4 cm.

**10-2 Developing Formulas for Circles and Regular Polygons** (*p 691*) 11-13, 15, 17, 22, 26, 30, 31, 33, 35, 38, 39, 41-44.

**Q:** What do you get when you divide a jack-o'-lantern's circumference by its diameter?

**A:** Pumpkin pi.

"The next best thing to solving a problem is finding some humor in it."—  
*Anonymous*

